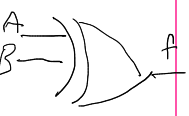


Optimization

Chapter 2 in the text

(Was Chapter 4 in the older texts)

EXCLUSIVE OR
XOR FOR



AB	f
00	0
01	1
10	1
11	0

K-maps
(Karnaugh)

Truth
Tables

There are different arrangements for showing all possibilities in combinations of inputs

Each region (or row) corresponds to a minterm or maxterm of the function

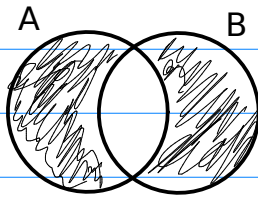
Different ways to represent a function

Venn Diagram

Two ways to do the labeling

2 variables:

A	B	f
0	0	0
0	1	1
1	0	1
1	1	0

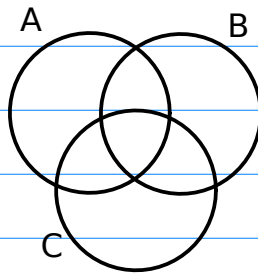


		A	
B	0	1	
	0	0	1
1	1	0	

B	A	
	0	1
0	0	1
1	1	0

3 variables:

A	B	C	f
0	0	0	
0	0	1	
0	1	0	
0	1	1	
1	0	0	
1	0	1	
1	1	0	
1	1	1	

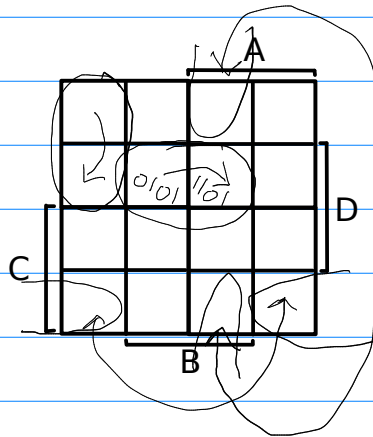


		A	
C	0	1	
	0	0	1
1	1	0	

C	AB			
	00	01	11	10
0	0	1	0	1
1	1	0	1	0

4 variables:

Remember: the order of the variables is significant: $f(A,B,C,D)$ would lay out differently from $f(D,C,B,A)$



CD	AB			
	00	01	11	10
00	0	1	0	1
01	1	0	1	0
11	0	1	0	1
10	1	0	1	0

5 variables:

$f(A,B,C,D,E)$
00000
00001
00010
00011
etc.

		B	
D	0	1	
	0	0	1
1	1	0	

		B	
D	0	1	
	0	0	1
1	1	0	

The book labels this differently

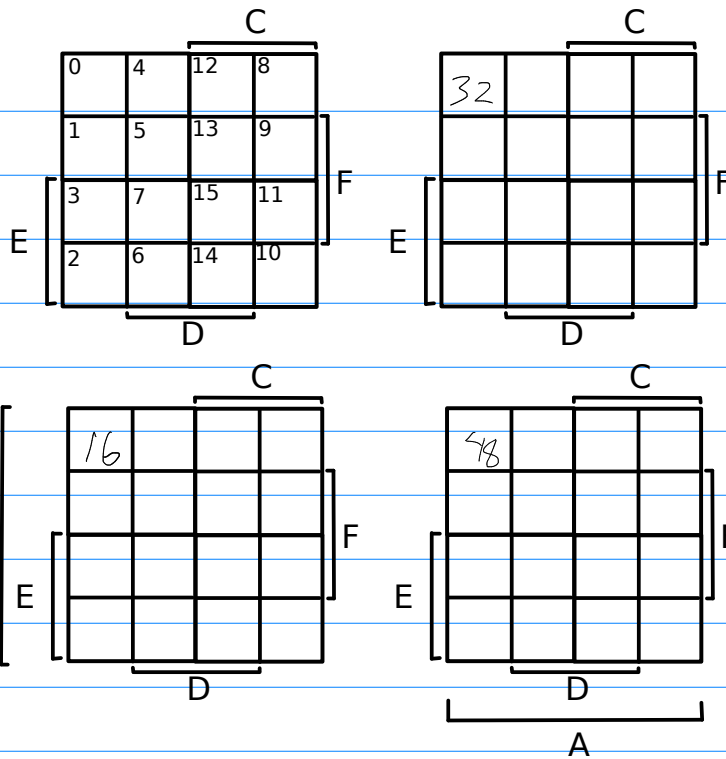
6 variables:

$ABCDEF$

$16 = 010000$

$32 = 100000$

$48 = 110000$

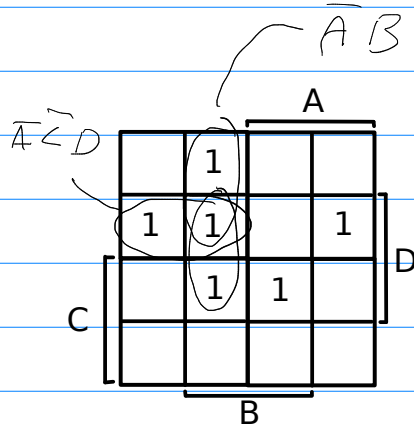


$B=1$

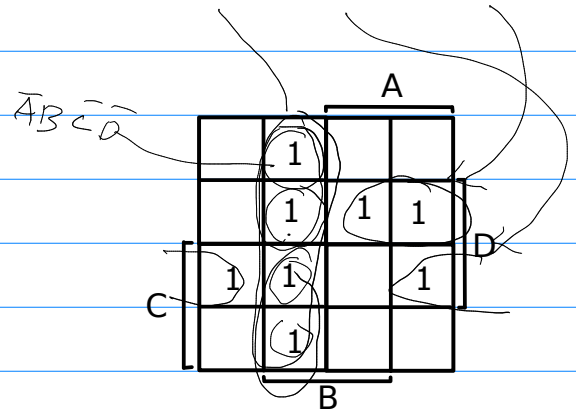
Representing a function in the K-map

$$f(A,B,C,D) = \sum m(1,4,5,7,9,15)$$

ABCD	f
0000	0
0001	1
0010	0
0011	0
0100	1
0101	1
0110	0
0111	1
1000	0
1001	1
1010	0
1011	0
1100	0
1101	0
1110	0
1111	1



$$f(A,B,C,D) = \bar{A}B + \bar{B}CD + A\bar{C}D$$



We usually only put in the 1's
(And leave out the 0's)